Lebanese university Faculty of Agriculture

## Entrance Exam 2020-2021 LS-Mathematics-Duration: 1h

Exercise 1

Consider the function  $f(x) = \frac{x^2 - 2}{(x+2)(x+1)}$ . Let (C) its graph in an orthonormal system  $(O, \overrightarrow{i}, \overrightarrow{j})$ .

- 1. Find the domain of definition D of the function f.
- 2. Calculate the limits of f at the bounds of its domain. What can we deduce?
- 3. Calculate f'(x) for all  $x \in D$ .
- 4. Set up the table of variations of f and draw (C).
- 5. Write f(x) in the form  $A + \frac{B}{x+2} + \frac{C}{x+1}$ , where A, B and C are real numbers to be determined
- 6. Calculate the area bounded by (C), the two lines x=2, x=3 and the x-axis.

Exercise 2

Calculate the following integrals:

$$1. \int \frac{\sqrt{e^x} + 1}{2e^x} \, \mathrm{d}x.$$

$$2. \int x^2 \ln(x) \, \mathrm{d}x.$$

$$3. \int \sqrt{2x+5} \, \mathrm{d}x.$$